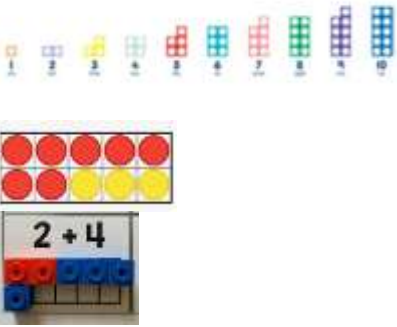
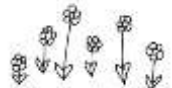

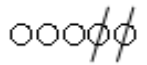
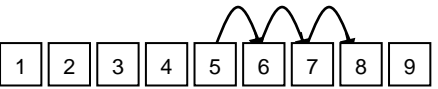
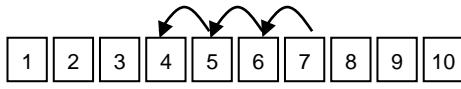
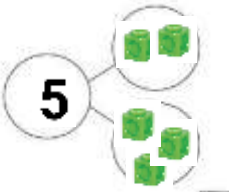
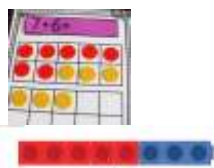
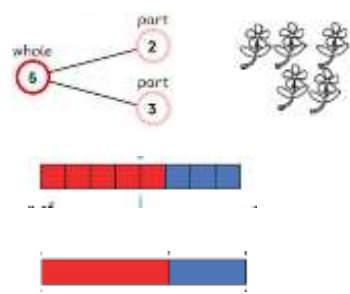
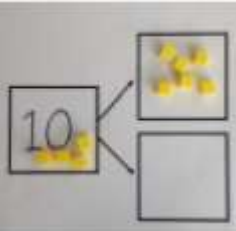
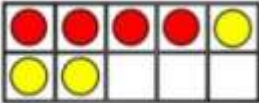
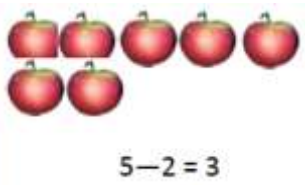
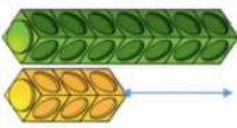
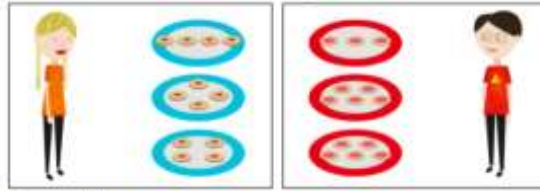


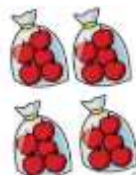
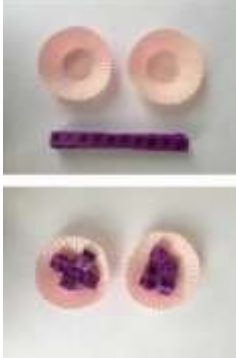
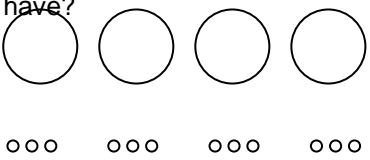
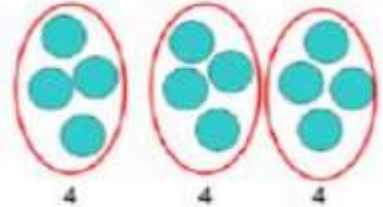
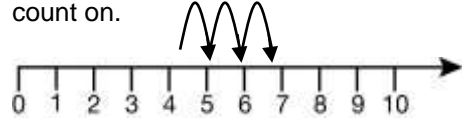


# Eliot Bank & Gordonbrock Calculation Policy

Addition	Subtraction	Multiplication	Division
<p><b>RECEPTION</b>  <b>Concrete</b>            Identify one more            Combine amounts to add            Find number bonds            Add without counting from the beginning</p>  <p><b>Pictorial</b></p>  <p><math>3 + 3 = 6</math></p>	<p><b>RECEPTION</b>  <b>Concrete</b>            Identify one less            Taking away using concrete objects e.g. <math>5 - 2 =</math></p>  <p><b>Pictorial</b></p> 		
<p><b>RECEPTION</b>            Using a completed number track to count on.</p> 	<p><b>RECEPTION</b>            Using a completed number track to count back.</p> 	<p><b>RECEPTION</b>            Grouping objects.</p> <p>Eg: <math>2 + 2 + 2 + 2 = 8</math></p> <p>4 groups of 2 = 8</p>	<p><b>RECEPTION</b>  <b>Sharing and grouping</b> objects.</p> <p>How many groups of 2 in 6?</p> <p style="text-align: center;"><math>= 3</math></p>

Addition	Subtraction	Multiplication	Division
<p><b>YEAR 1 Concrete</b> Part-part whole method and bar model with objects to add two numbers</p>  <p>Start with the bigger number and use the smaller number to make 10 on a tens frame, e.g. <math>7 + 6 =</math></p>  <p><b>Pictorial</b> Use pictures to add two numbers together using groups and as a bar</p> 	<p><b>YEAR 1 Concrete</b> Part-part whole method and bar model with objects to subtract two numbers</p>  <p>Using a tens frame and counters, take away corresponding number of counters to solve equations, e.g. <math>7 - 3 =</math></p>  <p>Using concrete objects to represent the bar model</p>  <p>Using concrete objects to find the difference</p> 	<p><b>YEAR 1 Concrete</b> Make equal groups using concrete objects</p>  <p>Add equal groups using concrete objects</p>  <p>Make equal rows using concrete objects</p>  <p><b>Pictorial</b> Count in steps verbally using pictorial representations</p> 	<p><b>YEAR 1 Concrete</b> Share equally using concrete objects</p>  <p><b>Sharing</b> 12 sweets between 4 groups...How many do each group have?</p>  <p><b>Pictorial</b></p>  <p><b>Abstract</b> 12 shared between 3 is 4</p> <p style="background-color: #90EE90; display: inline-block; padding: 2px;">COUNT IN 10s, 5s AND 2s.</p>

Using a completed number line to count on.

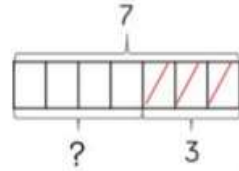


**Abstract**

$$5 + 12 = 17$$

Start with the bigger number. Use known facts e.g.  $5 + 2 = 7$  to make connections.

**Pictorial**



Using a completed number line to count back.



**Abstract**

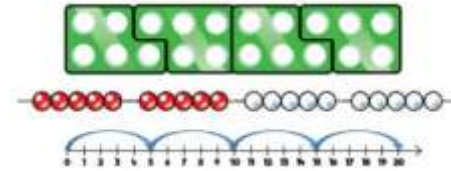
8	2
---	---

$$10 = 8 + 2$$

$$10 = 2 + 8$$

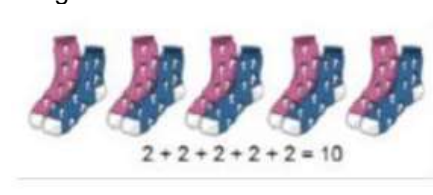
$$10 - 2 = 8$$

$$10 - 8 = 2$$



**Abstract**

Write addition sentences to represent pictorial images



Move on from using pictures to repeated addition number sentences

$$2 + 2 + 2 + 2 = 8$$

$$4 \text{ groups of } 2 = 8$$

$$4 \times 2$$

$$2 \times 4$$

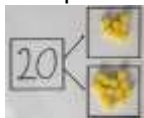

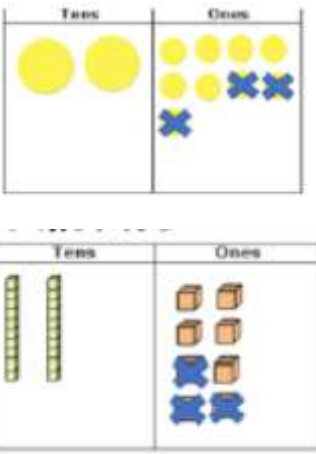

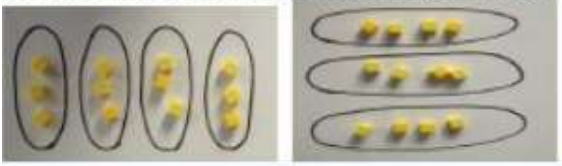
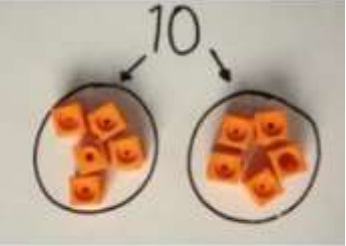
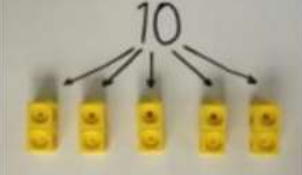
**COUNT IN 10s, 5s AND 2s.**

**YEAR 1 – with teacher support**  
**YEAR 2**

Record using **arrays**.

$$6 \times 2 =$$

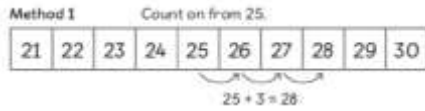
$$2 \times 6 =$$

Addition	Subtraction	Multiplication	Division
<p><b>YEAR 2</b> <b>Concrete</b></p> <p>Part-part whole method</p>  <p>Explore ways to partition any number up to 100</p>  <p><math>25 + 10 = 35</math></p> <p>Explore what happens to each digit when you add 10.</p>	<p><b>YEAR 2</b> <b>Concrete</b></p> <p>Using concrete counters and dienes to take away</p>  <p><b>Pictorial</b></p>	<p><b>YEAR 2</b> <b>Concrete</b></p> <p>Create arrays using cubes and numicon</p>  <p>Multiplication is commutative</p>  <p><b>Pictorial</b></p> <p>Use representations of arrays to show different calculations</p>	<p><b>YEAR 2</b> <b>Concrete</b></p> <p>Division by sharing using objects</p>  <p>Division by grouping using objects</p>  <p><b>Pictorial</b></p> <p>Using pictures for sharing</p>

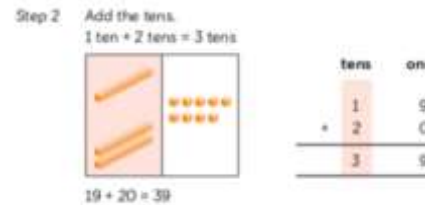
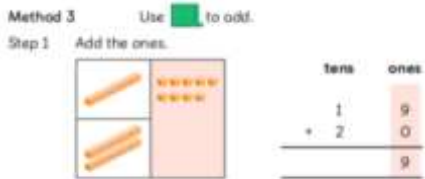


Model adding TO + TO using dienes, numicon and place value counters.

**Pictorial**

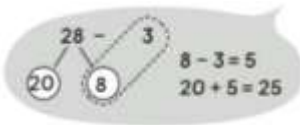
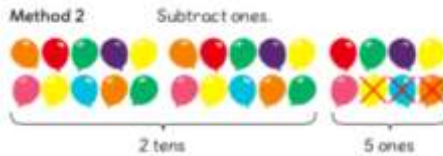
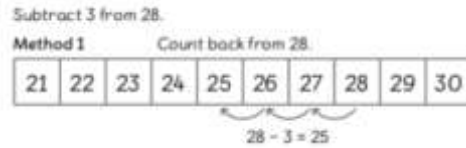
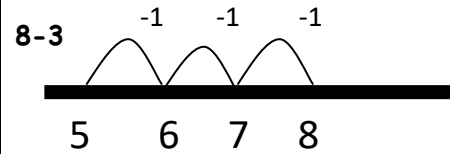


**Adding - no renaming**

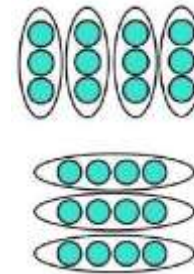
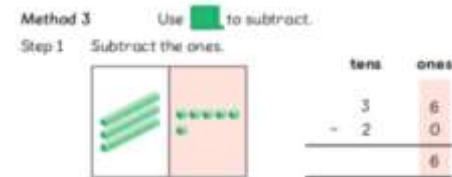


**Adding with renaming**

Using empty number line to count back in ones.



**Subtracting - no renaming**

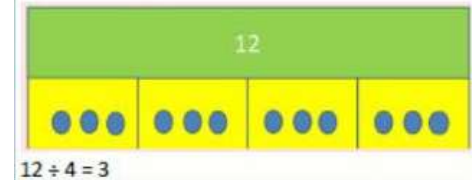
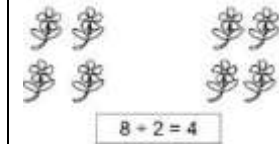


**Abstract**

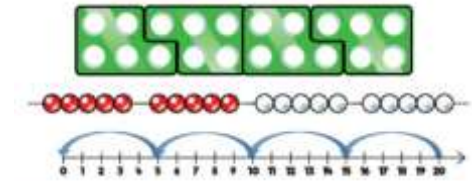
Use an array to write repeated addition and multiplication sentences



5 + 5 + 5 = 15  
 3 + 3 + 3 + 3 + 3 = 15  
 5 x 3 = 15  
 3 x 5 = 15



**Using pictures for grouping**

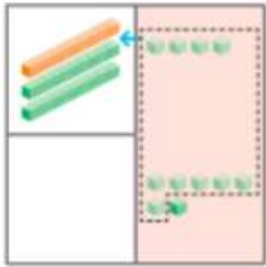



**Abstract**

12 ÷ 3 = 4

Model exchanging 10 ones for one ten

Step 1 Add the ones.  
 $4 \text{ ones} + 7 \text{ ones} = 11 \text{ ones}$   
 Regroup the ones.  
 $11 \text{ ones} = 1 \text{ ten and } 1 \text{ one}$

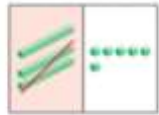


Use  to help you add.

	tens	ones
	2	4
+		7
	1	1



Step 2 Subtract the tens.  
 $3 \text{ tens} - 2 \text{ tens} = 1 \text{ ten}$

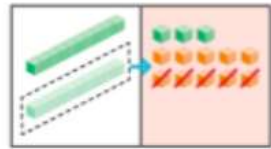


$36 - 20 = 16$

	tens	ones
	3	6
-	2	0
	1	6

Subtracting with renaming

Step 1 Regroup 1 ten into 10 ones.  
 Subtract the ones.  
 $13 \text{ ones} - 5 \text{ ones} = 8 \text{ ones}$

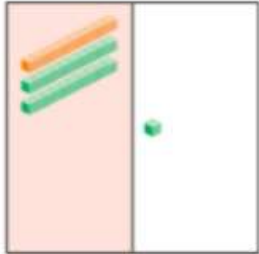


	tens	ones
	1	3
-		5
		8

$13 - 5 = 8$



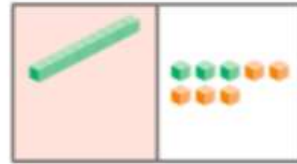
Step 2 Add the tens.  
1 ten + 2 tens = 3 tens



$$24 + 7 = 31$$

	tens	ones
	2	4
+		7
	1	1
+	2	0
	3	1

Step 2 Subtract the tens.



$$23 - 5 = 18$$

	tens	ones
	1	3
-		5
	1	8

10 - 0 = 10



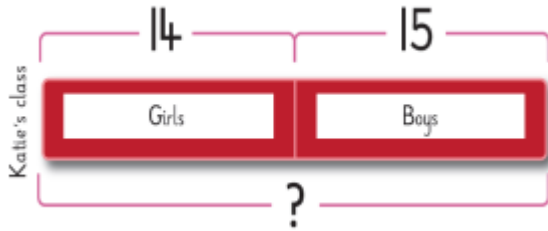
**Year 2**

**Abstract**

**Addition**

**Part Whole Model**

There are 14 girls and 15 boys in Katie's class.  
How many children are in the class altogether?



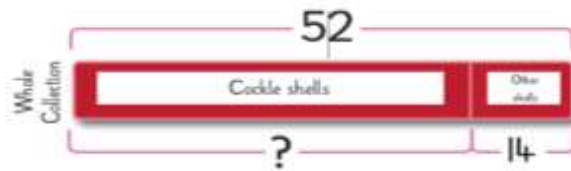
**Year 2**

**Abstract**

**Subtraction**

**Part Whole Model**

Denise collects seashells from the beach when she goes on her holiday. She has 52 beautiful seashells. Most of them are cockle-shells. There are 14 shells of other kinds.  
How many are cockle-shells?





## Addition

**YEAR 3**  
**Concrete**

Addition - no renaming  
Model using dienes and numicon  
Always add the ones first

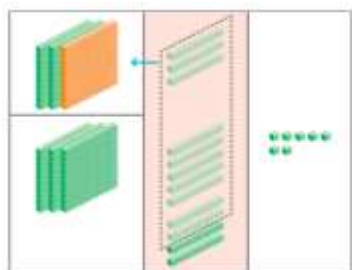


$432 + 521 = 953$

Move on to using place value counters



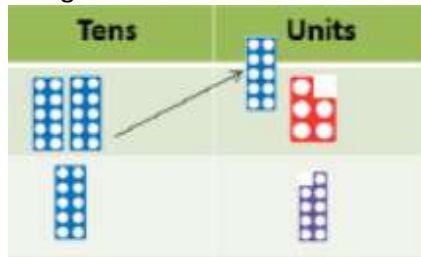
Addition with renaming



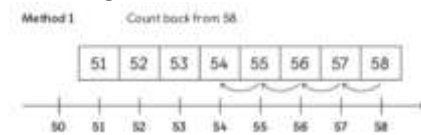
## Subtraction

**YEAR 3**  
**Concrete**

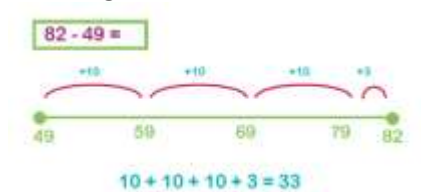
Using base 10 or numicon to model



**Pictorial**  
Counting back



Counting on



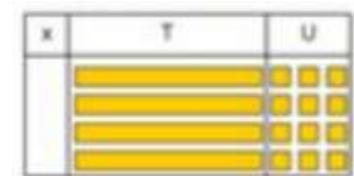
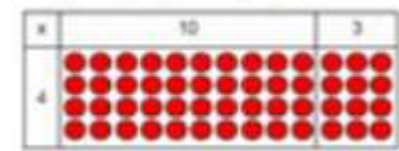
Method 2 Subtract ones



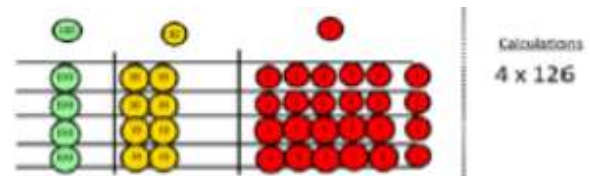
## Multiplication

**YEAR 3**  
**Concrete**

Use counters and dienes to introduce the grid method



Fill each row with 126 to represent the calculation 126 x 4



Calculations  
 $4 \times 126$

Add up each of the columns, starting with the ones, making any exchanges needed

## Division

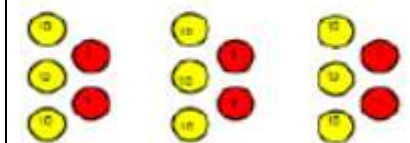
**YEAR 3**  
**Concrete**

Using numicon and concrete resources to divide by **grouping**

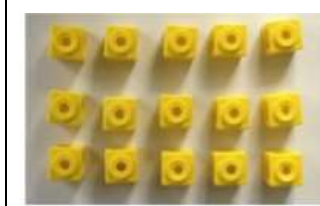
24 divided into groups of 6 = 4



$96 \div 3 = 32$



Using arrays to complete number facts



Eg  $15 \div 3 = 5$     $5 \times 3 = 15$   
 $15 \div 5 = 3$     $3 \times 5 = 15$

	h	t	o
	1	3	6
+	3	9	1
<hr/>			
		2	7

Add the ones  
 Add the tens  
 $3 \text{ tens} + 9 \text{ tens} = 12 \text{ tens}$   
 Regroup the tens  
 $12 \text{ tens} = 1 \text{ hundred} + 2 \text{ tens}$

**Pictorial**

Method 1 Count on from 213.

211 212 213 214 215 216 217 218 219 220

213 + 4 = 217

Method 2 Add the ones.

213 + 4 = 217

3 + 4 = 7  
 $210 + 7 = 217$

Draw counters using place value charts when adding two numbers

**Subtracting without renaming**

Subtract the ones.  
 $3 \text{ ones} - 3 \text{ ones} = 0 \text{ ones}$

h	t	o
	3	3
		- 3
<hr/>		
	3	0

Subtract the tens.  
 $7 \text{ tens} - 2 \text{ tens} = 5 \text{ tens}$

h	t	o
	7	3
		- 20
<hr/>		
	5	3

Subtract the hundreds.  
 $8 \text{ hundreds} - 7 \text{ hundreds} = 1 \text{ hundred}$

h	t	o
8	3	3
	7	3
<hr/>		
1	0	0

$895 - 733 = 162$   
 There were 162 beads left in the jar.

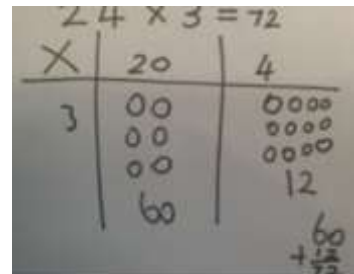
**Subtracting with renaming**

Step 1: Regroup 1 ten into 10 ones.  
 Subtract the ones.  
 $11 \text{ ones} - 6 \text{ ones} = 5 \text{ ones}$

h	t	o
	2	13
		- 6
<hr/>		
	1	7

**Pictorial**

Children draw pictures of counters to represent the grid method



**Abstract**

**IMPORTANT:** In order to move on to the next stage, children MUST be able to...

- 1) multiply any number by 10
- 2) multiply any number by 100
- 3) multiply 1 digit by a multiple of 10 ( $5 \times 30$ ) and multiple of 100 ( $4 \times 600$ )
- 4) Multiply multiples of 10 ( $20 \times 50$ )

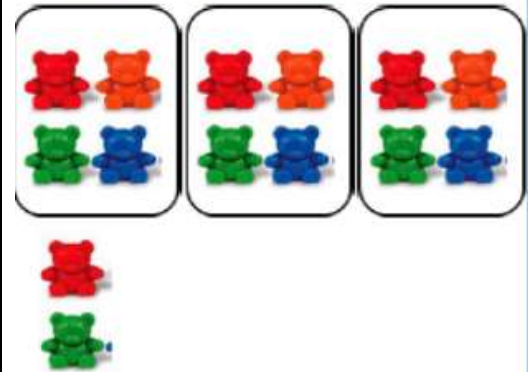
Use partitioning method, then addition

$43 \times 5 =$

$40 \times 5 = 200$   
 $3 \times 5 = 15$   
 $200 + 15 = 215$

$14 \div 3 =$

Divide objects between groups and see how much is left over



**Pictorial**

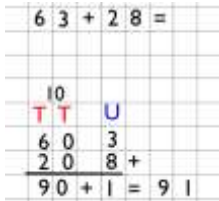


20

$20 \div 5 = ?$   
 $5 \times ? = 20$



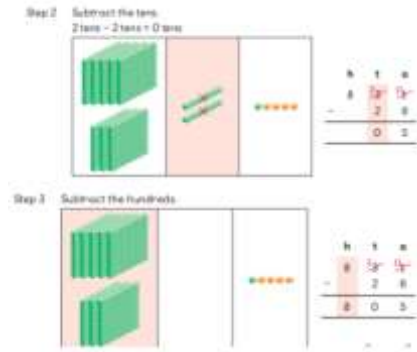
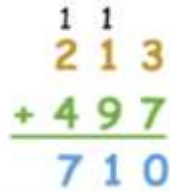
**Abstract**



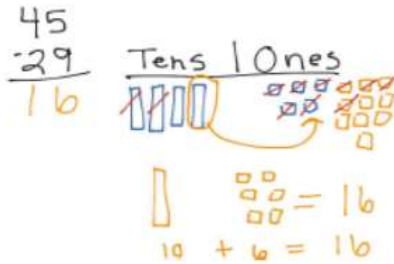
Without renaming:



With renaming:

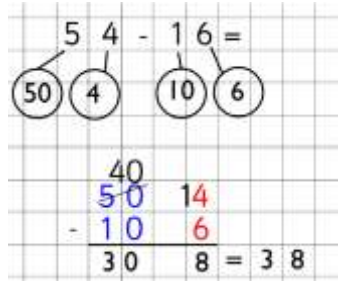


Children may draw base 10 and show the exchanging



**Abstract**

Partition into place value columns



Move on to formal method

Using the written grid method

x	30	5
7	210	35

$210 + 35 = 245$

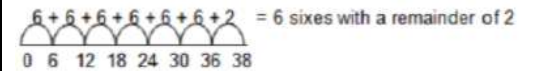
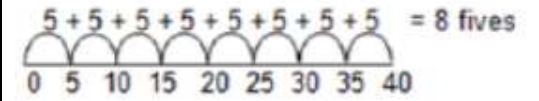
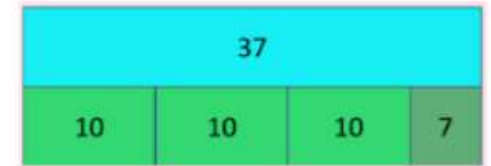
Multiplication as **repeated addition** using an **empty** number line:  $5 \times 2$

**LEARN TIMES TABLES 3 x 4x 8x**

Draw dots and group them to divide an amount and clearly show a remainder.



Use bar models to show division with remainders.



**Abstract**



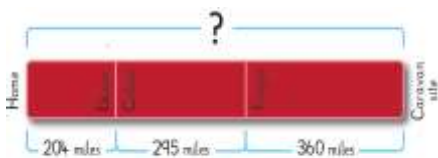
**LEARN DIVISION FACTS FOR X3 X 4 X8**

$$\begin{array}{r}
 728 - 582 = 146 \\
 \begin{array}{r}
 \text{H} \quad \text{T} \quad \text{U} \\
 \cancel{7} \quad 2 \quad 8 \\
 5 \quad 8 \quad 2 \\
 \hline
 1 \quad 4 \quad 6
 \end{array}
 \end{array}$$

## Singapore Maths (Bar Model)

### Year 3 Addition Part Whole Model

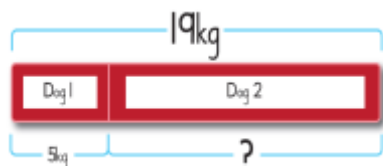
Richard's family went to a caravan in the South of France for their summer holiday. Richard's Dad drove 204 miles to Dover on Wednesday morning; then the ferry carried them to Calais in France. From Calais, Richard's Dad drove 295 miles to Troyes where the family stayed overnight. On Thursday morning, he drove the final 360 miles to their caravan site. How far did Richard's Dad drive altogether?



### Comparison Model

### Year 3 Subtraction Part Whole Model

Two dogs weigh 19kg. The first dog weighs 5kg. How much does the second dog weigh?



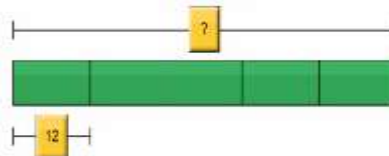
### Comparison Model

Tom and Finley were sorting the wheeled toys in the outdoor area. They found 13 tractors and 17 diggers. How many more diggers were there than tractors?



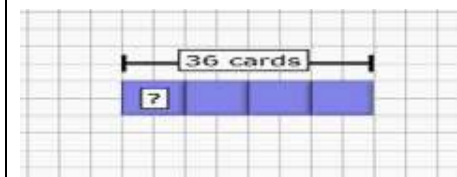
### Year 3 Multiplication

There are 12 pencils in a pack. Shirley gives out 5 packets of pencils. How many pencils does she give out altogether?



### Year 3 Division

Kelly has 36 Lego cards. She sorted them into 4 equal piles. How many Lego cards were in each pile?



Sam had 13 Pokemon cards. Jim had 21 more cards than Sam. How many Pokemon cards does Jim have?



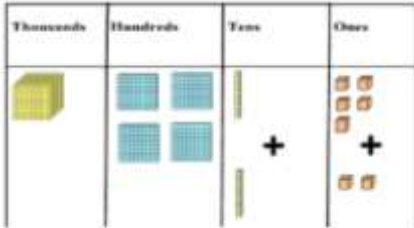
## Addition

**YEAR 4**

**Concrete**

Column addition

Using dienes and place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand



Use counters and a place value grid to calculate  $3242 + 2213$

1000s	100s	10s	1s
3	2	4	2
2	2	1	3

**Pictorial**

Using pictures to move on to abstract column addition method

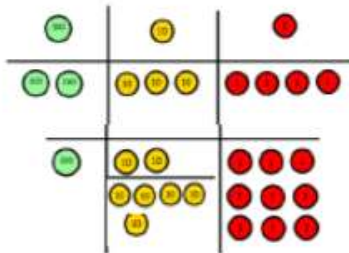
## Subtraction

**YEAR 4**

**Concrete**

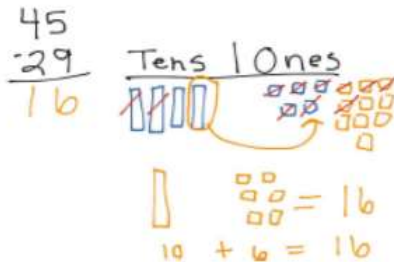
Model process of exchanging using dienes and numicon. Then move on to using place value counters

$$234 - 179$$



**Pictorial**

Draw to show the exchange using dienes or place value counters



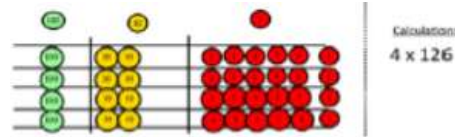
## Multiplication

**YEAR 4**

**Concrete**

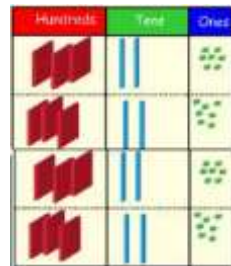
Recap using concrete resources to represent the grid method

Fill each row with 126 to represent the calculation  $126 \times 4$



Add up each of the columns, starting with the ones, making any exchanges needed

Use dienes to represent column multiplication - multiply the ones first



## Division

**YEAR 4**

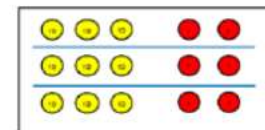
**Concrete**

Use place value counters to divide by a single digit number

$$96 \div 3$$

Tens      Units  
3            2

3



Rose uses counters to find the total of 3,356 and 2,435

Th	H	T	O
3	3	5	6
+	2	4	3
5	7	9	1

Use Rose's method to calculate:  
 $3,356 + 2,437$     $3,356 + 2,473$     $3,356 + 2,743$

**Abstract**

**Column addition:**

Without renaming:

$$\begin{array}{r} 1415 \\ + 12 \\ \hline 1427 \end{array}$$

With renaming:

$$\begin{array}{r} 11 \\ 1415 \\ + 96 \\ \hline 1511 \end{array}$$

**Extend to decimals - double check if adding decimals is in the year 4 curriculum**

IMPORTANT: Children must understand how to insert zeros as place holders when dealing with decimal numbers.

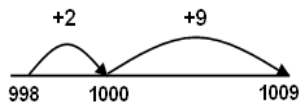
**Abstract**

**Column subtraction**

**\*\*Always start with ones\*\* exchange only for units, then tens, then both\*\* extend to thousands etc\*\* extend to decimals\*\* - check Y4 curriculum for this**

$$\begin{array}{r} 614 \\ - 86 \\ \hline 668 \end{array}$$

IMPORTANT: Do not use columns to subtract from a number with **lots of zeros** or when numbers are **close together**...teach the children to let the numbers determine the best method: **1009 - 998 = 11**



**Pictorial**

Recap drawing counters to represent the grid method

$24 \times 3 = 72$

x	300	20	7
4	1200	80	28

**Abstract**

Short expanded method

$$\begin{array}{l} 127 \times 6 = 762 \\ 42 \quad (6 \times 7) \\ + 120 \quad (6 \times 20) \\ \hline 600 \quad (6 \times 100) \\ \hline 762 \end{array}$$

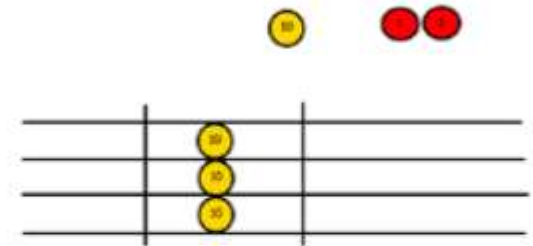
Move on to short formal method

	H	T	O
x	2	4	7
	9	8	0
	1	2	

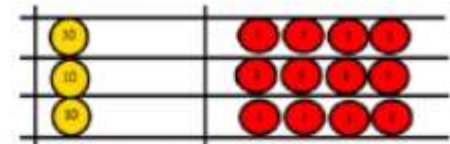
**LEARN TIMES TABLES X6 X7 X9 X11 X12**

$42 \div 3 =$

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



We exchange this ten for ten ones and then share the ones equally among the groups.

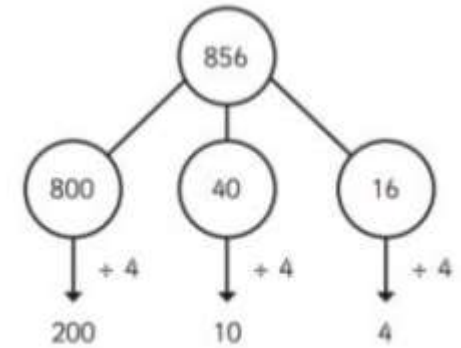


We look how much in 1 group so the answer is 14.

**Pictorial**

844

844			
?	?	?	?



**Abstract**

$$98 \div 7 = 14$$

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \end{array}$$

...and with remainders

$$432 \div 5 = 86 \text{ r}2$$

$$\begin{array}{r} 086 \text{ r}2 \\ 5 \overline{) 432} \end{array}$$

LEARN DIVISION FACTS FOR X 6 x 7 x9 X11 X12

**Year 4**

**Abstract**

**Addition**

**Part Whole Model**

The population of a village was 5678. Then, it increased by 1235 people. What was the population of the village after the increase?



**Comparison Model**

David has collected 125 Lego cards. Harry has 85 more cards. How many cards does Harry have?



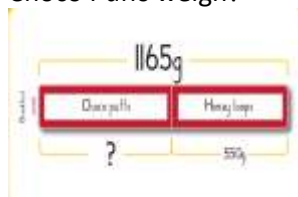
**Year 4**

**Abstract**

**Subtraction**

**Part Whole Model**

There are two boxes of breakfast cereal in Adam's basket. Together they weigh 1165g. The Honey Loops are 550g. What do the Choco Puffs weigh?



**Comparison Model**

There are 405 apples and 372 oranges. How many more apples than oranges are there?

Find the difference.



The difference is

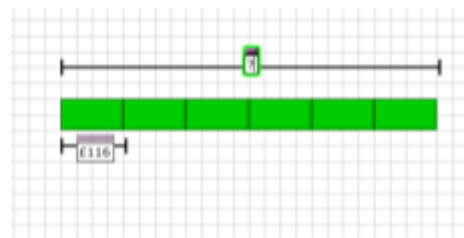
**Year 4**

**Abstract**

**Multiplication**

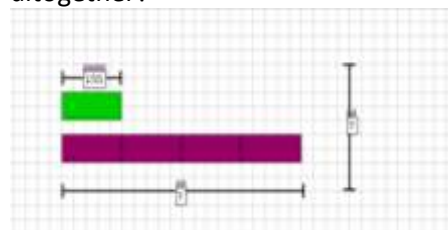
**Part Whole Model**

Each ticket from London to Manchester costs £116. How much will 6 tickets cost from London to Manchester?



**Comparison Model**

Lulu has 155 beads. Holly has 4 times as many beads as Lulu has. How many beads do Lulu and Holly have altogether?



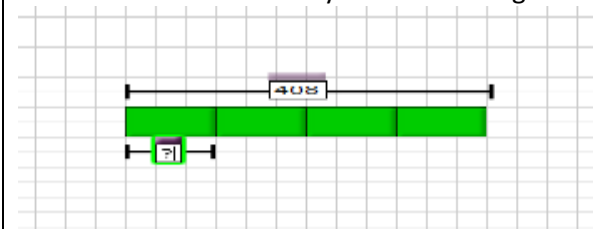
**Year 4**

**Abstract**

**Division**

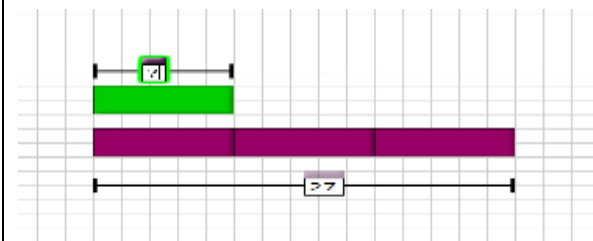
**Part Whole Model**

Jenny made 408 chocolate cakes to sell. She put them into boxes of 4. How many boxes did she get?



**Comparison Model**

There are 27 red flowers. There are 3 times as many red flowers as white flowers. How many white flowers are there?





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## Addition

**YEAR 5 & YEAR 6**  
Continue using methods from Y4 for adding whole numbers  
Introduce adding decimals

**Concrete**

**Pictorial**

$$3.65 + 2.41 = 6.06$$

## Subtraction

**YEAR 5 & YEAR 6**  
Continue using methods from Y4 subtraction with and without renaming.  
Introduce subtracting decimals

**Concrete**  
Use place value counters

**Pictorial**

$$5.43 - 2.7 = 2.73$$

**Abstract**

## Multiplication

**YEAR 5 & YEAR 6**  
**Concrete**  
Multiply the ones first

**Pictorial**

x	300	20	7
4	1200	80	28

**Abstract**  
Expanded long multiplication

$$23 \times 13 = 299$$

$$\begin{array}{r} 23 \\ \times 13 \\ \hline 69 \quad (3 \times 3) \\ 60 \quad (3 \times 20) \\ + 30 \quad (10 \times 3) \\ \hline 200 \quad (10 \times 20) \\ 299 \end{array}$$

Moving on to formal long multiplication

## Division

**YEAR 5 & YEAR 6**  
**Concrete**  
 $42 \div 3 =$

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

We exchange this ten for ten ones and then share the ones equally among the groups.

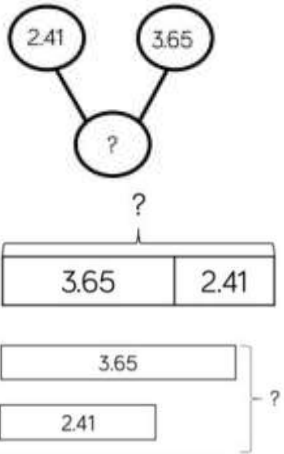
We look how much in 1 group so the answer is 14.

**Pictorial**

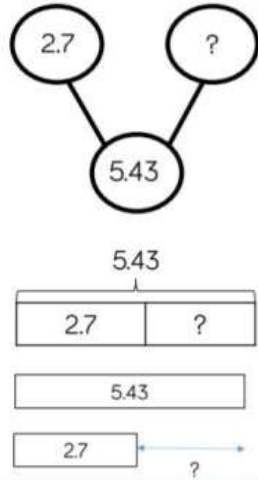
division by chunking on a numberline  
 $96 \div 4 = 24$

How many lots of 4 sit together?  
 $10 + 10 + 4 = 24$

**Abstract**



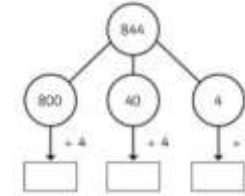
$$\begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ 1 \end{array}$$



$$\begin{array}{r} 4 \ 1 \\ 5.43 \\ + 2.7 \\ \hline 2.73 \end{array}$$

$56 \times 27 = 1512$

$$\begin{array}{r} 56 \\ \times 27 \\ \hline 392 \\ + 1120 \\ \hline 1512 \\ 1 \end{array}$$



**Abstract**

$256 \div 7 = 36 \text{ R}4$

$$\begin{array}{r} 256 \\ - 140 \quad (20 \times 7) \\ \hline 116 \\ - 70 \quad (10 \times 7) \\ \hline 46 \\ - 42 \quad (6 \times 7) \\ \hline 4 \end{array}$$

Family of

- Facts:  
 $20 \times 7 = 140$   
 $10 \times 7 = 70$   
 $5 \times 7 = 25$   
 $2 \times 5 = 10$   
 $1 \times 5 = 5$

**Long Division (bus stop method)**

$8764 \div 4 = 2191$

$$\begin{array}{r} 2191 \\ 4 \overline{)8764} \\ \underline{8} \phantom{00} \\ 07 \phantom{00} \\ \underline{4} \phantom{00} \\ 36 \phantom{00} \\ \underline{36} \phantom{00} \\ 04 \phantom{00} \\ \underline{4} \phantom{00} \\ 0 \end{array}$$

$546 \div 31 = 17 \text{ r}19$

$$\begin{array}{r} 17 \text{ r}19 \\ 31 \overline{)546} \\ \underline{31} \phantom{00} \\ 236 \phantom{00} \\ \underline{217} \phantom{00} \\ 19 \end{array}$$

**Short Division (bus stop method)**

	97
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			<table border="1"> <tr> <td>3</td> <td>2 9<sup>2</sup>1</td> </tr> </table> <p>General Rule:  When dividing by a single digit = bus stop  When dividing by a double digit = vertical chunking... then long division</p>	3	2 9 <sup>2</sup> 1
3	2 9 <sup>2</sup> 1				
<b>Singapore Maths (Bar Model)</b>					
<b>Year 5 &amp; 6</b> <u>As Above</u>	<b>Year 5 &amp; 6</b> <u>As above</u>	<b>Year 5 &amp; 6</b> <u>As above</u>	<b>Year 5 &amp; 6</b> <u>As above</u>		